

## Week 5 – part 3b :Poisson Model



# Neuronal Dynamics: Computational Neuroscience of Single Neurons

## Week 5 – Variability and Noise: The question of the neural code

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✓ 5.1 Variability of spike trains  
- experiments

✓ 5.2 Sources of Variability?  
- Is variability equal to noise?

5.3 Three definitions of Rate code  
- Poisson Model

5.4 Stochastic spike arrival  
- Membrane potential fluctuations

5.5. Stochastic spike firing  
- subthreshold and superthreshold

## Week 5 – part 3b :Poisson Model



✓ **5.1 Variability of spike trains**  
- experiments

✓ **5.2 Sources of Variability?**  
- Is variability equal to noise?

**5.3 Three definitions of Rate code**

- Poisson Model

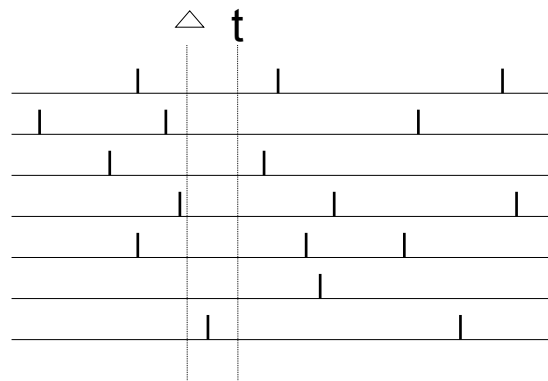
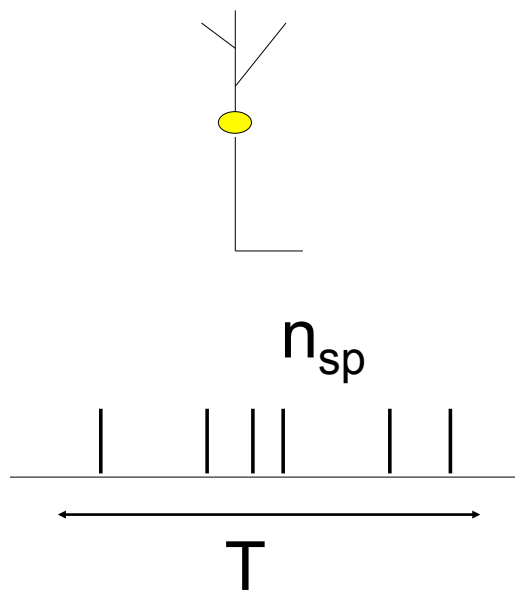
**5.4 Stochastic spike arrival**

- Membrane potential fluctuations

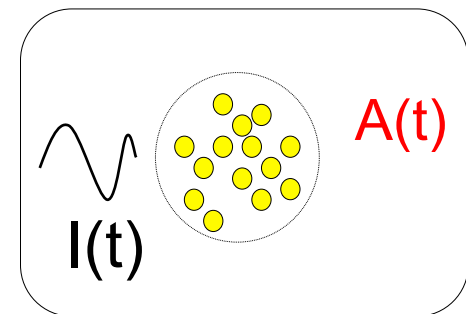
**5.5. Stochastic spike firing**

- subthreshold and superthreshold

## Neuronal Dynamics – 5.3b. Inhomogeneous Poisson Process



$$PSTH(t) = \frac{n(t; t + \Delta t)}{K \Delta t}$$



$$A(t) = \frac{n(t; t + \Delta t)}{N \Delta t}$$

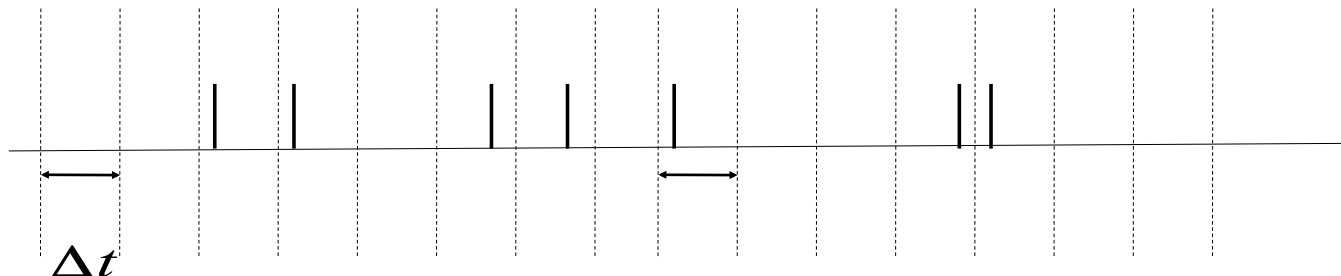
population  
activity

Pure rate code = stochastic spiking  $\rightarrow$  Poisson model

## Neuronal Dynamics – 5.3b. Poisson Model

Homogeneous Poisson model: constant rate

*Math detour:  
Poisson model*



Probability of finding a spike  $P_F = \rho_0 \Delta t$

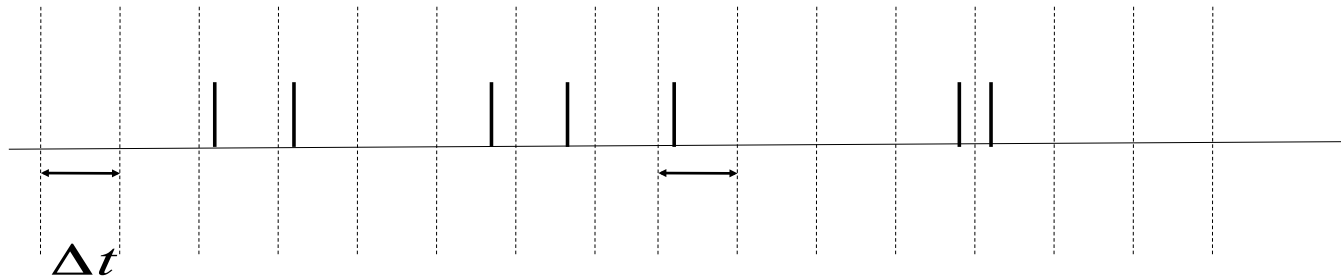
Pure rate code = stochastic spiking  $\rightarrow$  Poisson model

## Neuronal Dynamics – 5.3b. Poisson Model

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Probability of firing:

$$P_F = \rho_0 \Delta t$$



Take  $\Delta t \rightarrow 0$

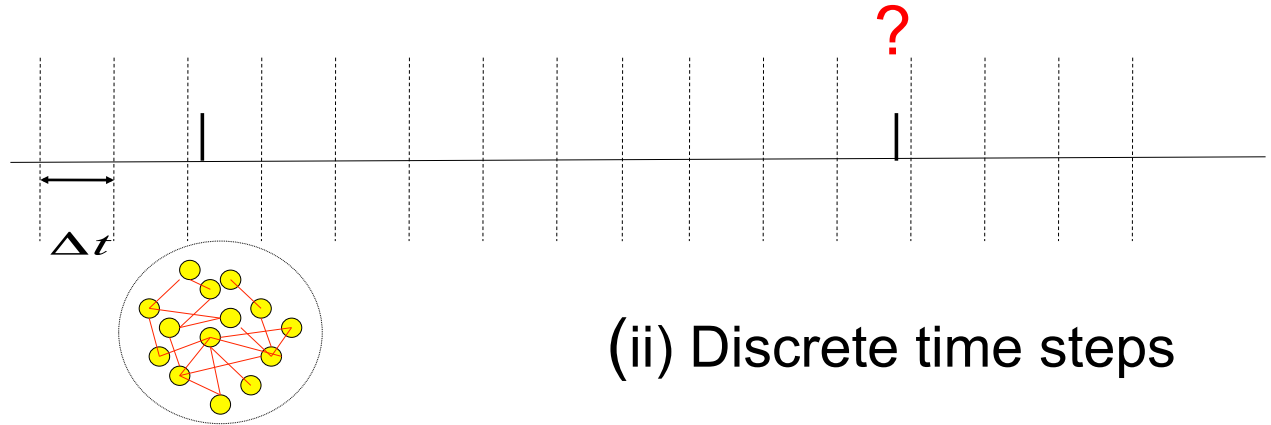
## Neuronal Dynamics – 5.3b. Interval distribution

Probability of firing:

$$P_F = \rho_0 \Delta t$$

(i) Continuous time

*prob to 'survive'*

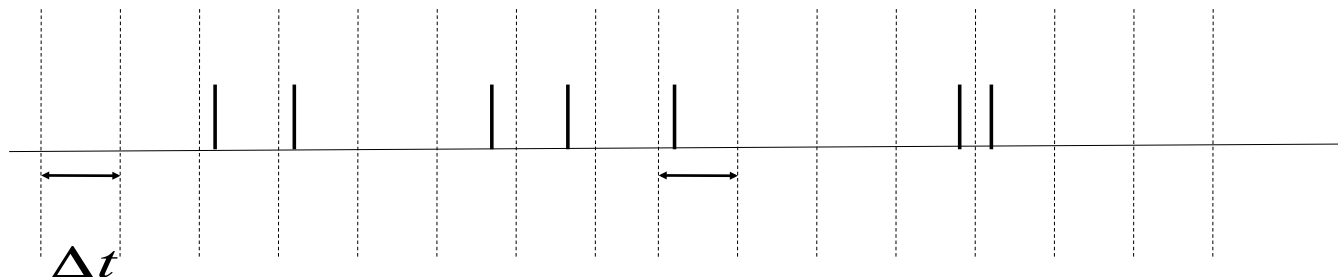


(ii) Discrete time steps

$$\Delta t \rightarrow 0$$

## Neuronal Dynamics – 5.3b. Inhomogeneous Poisson Process

rate changes

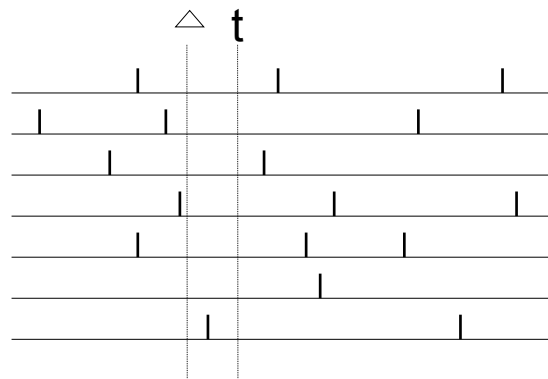
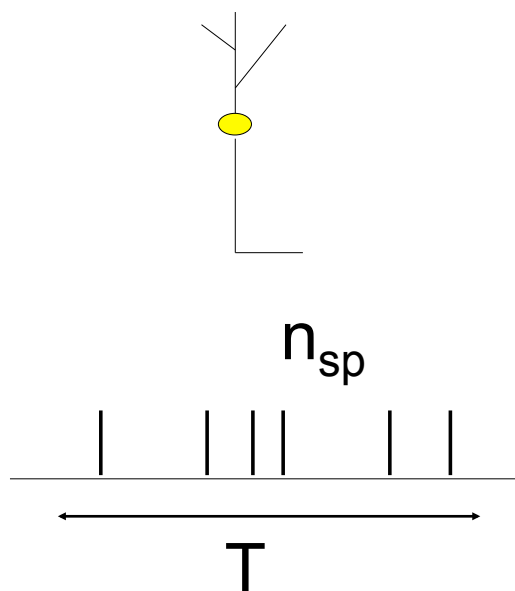


Probability of firing  $P_F = \rho(t) \Delta t$

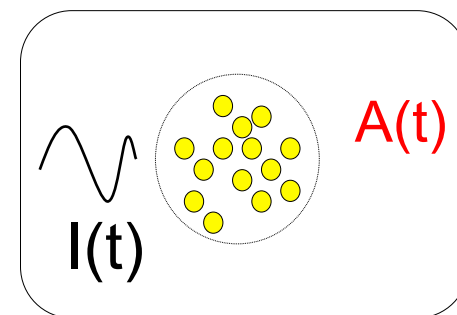
Survivor function  $S(t | \hat{t}) = \exp\left(-\int_{\hat{t}}^t \rho(t') dt'\right)$

Interval distribution

# Neuronal Dynamics – 5.3b. Inhomogeneous Poisson Process



$$PSTH(t) = \frac{n(t; t + \Delta t)}{K \Delta t}$$



$$A(t) = \frac{n(t; t + \Delta t)}{N \Delta t}$$

population  
activity

inhomogeneous Poisson model consistent with rate coding



## Neuronal Dynamics – 5.3b. Inhomogeneous Poisson Process

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Probability of firing

$$P_F = \rho(t) \Delta t$$

Survivor function

$$S(t | \hat{t}) = \exp\left(-\int_{\hat{t}}^t \rho(t') dt'\right)$$

Interval distribution

$$P(t | \hat{t}) = \rho(t) \exp\left(-\int_{\hat{t}}^t \rho(t') dt'\right)$$

## Neuronal Dynamics – Quiz 5.3.

### A Homogeneous Poisson Process:

A spike train is generated by a homogeneous Poisson process with rate 25Hz with time steps of 0.1ms.

- ☐ The most likely interspike interval is 25ms.
- ☐ The most likely interspike interval is 40 ms.
- ☐ The most likely interspike interval is 0.1ms
- ☐ We can't say.

### B Inhomogeneous Poisson Process:

A spike train is generated by an inhomogeneous Poisson process with a rate that oscillates periodically (sine wave) between 0 and 50Hz (mean 25Hz). A first spike has been fired at a time when the rate was at its maximum. Time steps are 0.1ms.

- ☐ The most likely interspike interval is 25ms.
- ☐ The most likely interspike interval is 40 ms.
- ☐ The most likely interspike interval is 0.1ms.
- ☐ We can't say.