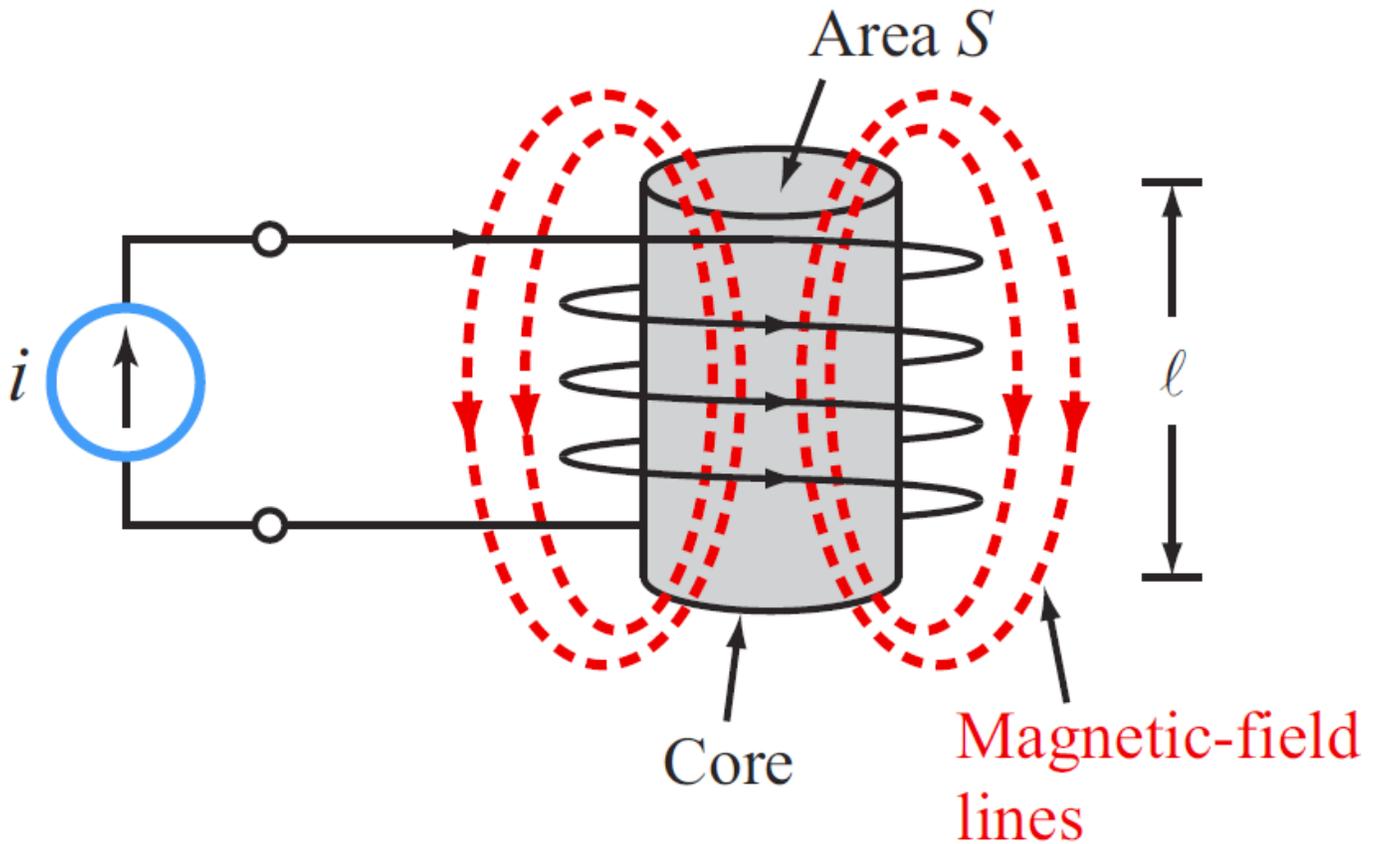


## Inductors

Capacitors and inductors constitute a canonical pair of devices. Whereas capacitors can store energy through the electric field induced by the voltage imposed across its terminals, **inductors** can store magnetic energy through the magnetic field induced by the current flowing through its wires.



Just as with capacitors, many geometries give rise to an inductance; in general, any current flowing through a wire produces a magnetic field, which in turn is seen as an inductance on that wire. The solenoid geometry pictured above is a good canonical case that illustrates the trends in dependence on geometry and material properties. The solenoid consists of multiple turns of wire wound in a helical geometry around a cylindrical core. The core may be air filled or may contain a magnetic material with magnetic permeability  $\mu$ . If the wire carries a current  $i(t)$  and the turns are closely spaced, the solenoid produces a relatively uniform magnetic field  $B$  within its interior region. The inductance of a solenoid of length  $\ell$  and cross-sectional area  $S$  is

$$L = \frac{\mu N^2 S}{\ell}$$

where  $N$  is the number of turns and  $\mu$  is the magnetic permeability of the core material.

Magnetic-flux linkage  $\Lambda$  is defined as the total magnetic flux linking a coil or a given circuit. For a solenoid with  $N$  turns carrying a current  $i$ :

$$\Lambda = \left( \frac{\mu N^2 S}{\ell} \right) i \quad (\text{Wb})$$

The unit for  $\Lambda$  is the weber (Wb), named after the German scientist Wilhelm Weber (1804–1891).

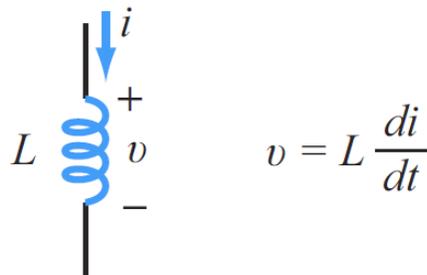
According to Faraday's law, if the magnetic-flux linkage in an inductor (or circuit) changes with time, it induces a voltage  $v$  across the inductor's terminals given by

$$v = \frac{d\Lambda}{dt}$$

Combining the above,

$$v = \frac{d}{dt} (Li) = L \frac{di}{dt}$$

Thus, the symbol for an inductor and the i-v definition is given below:



### What is permeability, $\mu$ ?

The relative magnetic permeability  $\mu_r$  is defined as

$$\mu_r = \frac{\mu}{\mu_0}$$

where  $\mu_0 \approx 4\pi \times 10^{-7}$  (H/m) is the magnetic permeability of free space.

Except for ferromagnetic materials,  $\mu_r \sim 1$  for all dielectrics and conductors. The  $\mu_r$  of ferromagnetic materials (which include iron, nickel, and cobalt) can be as much as five orders of magnitude larger than that of other materials.

Consequently,  $L$  of an iron-core solenoid is about 5000 times that of an air-core solenoid of the same size and shape.

Material	relative Permeability $\mu_r$
<b>All Dielectrics and Non-Ferromagnetic Metals</b>	$\approx 1.0$
<b>Ferromagnetic Metals</b>	
<b>Cobalt</b>	250
<b>Nickel</b>	600
<b>Mild steel</b>	2,000
<b>Iron (pure)</b>	4,000–5,000
<b>Silicon iron</b>	7,000
<b>Mumetal</b>	$\sim 100,000$
<b>Purified iron</b>	$\sim 200,000$

Some material reproduced with permission from Ulaby, F. T., & Maharbiz, M. M. (2012). *Circuits*. 2<sup>nd</sup> Edition, NTS Press.